Convex Optimization – Questions for the Exam Fall Semester 2021/2022

- 1. Linear and affine subspaces, convex sets and cones in linear spaces. Set theoretic operations and algebraic operations with such sets.
- 2. Linear, affine, cone and convex combinations, The characterization of the linear, affine, convex cone and convex hull of sets.
- 3. The generalized drop theorem for the computation of the convex hull of the union of convex sets. Half spaces and the Stone separation theorem.
- 4. Linear and affine functions, convex and sublinear functions and their characterizations. Implications among these properties.
- 5. The core (algebraic interior) of convex sets and its properties. Hyperplanes and the halfspaces determined by hyperplanes.
- 6. Separation of disjoint convex sets by hyperplanes or affine functions.
- 7. The sandwich theorem for convex-concave pairs of functions.
- 8. Topological vector spaces. The connection between the core and the topological interior of sets. The interior and the closure of convex sets and convex cones.
- 9. Characterization of continuity of convex functions. Local Lipschitz property of regular convex functions. The continuity of convex functions over finite dimensional spaces.
- 10. Directional derivative of convex functions and its basic properties. Global Lipschitz property the directional derivative of regular convex functions.
- 11. The subgradient of convex functions. Connection between the subgradient and the directional derivative.
- 12. The sum rule for the directional derivative and for the subgradient of convex functions.
- 13. The maximum theorem. The directional derivative and the subgradient of the maximum of convex functions.
- 14. Local and global minimum point for convex functions. The Fermat principle.
- 15. Minimum problems with convex inequality constraints. Necessary and sufficient conditions: The Karush–Kuhn–Tucker multiplier theorem.